# Fluctuating magnetic droplets immersed in a sea of quantum spin liquid

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# **GRAPHICAL ABSTRACT**



# **PUBLIC SUMMARY**

- Multiple techniques are used to study QSL candidate NaYbSe<sub>2</sub>.
- The absence of long-range magnetic order is confirmed by all techniques.
- Coexistence of quasi-static and dynamic spins is observed in both μSR and NMR.
- Results of thermal conductivity suggest the absence of itinerant gapless magnetic excitations.
- A scenario of fluctuating ferrimagnetic droplets immersed in a sea of QSL is proposed.



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The search of quantum spin liquid (QSL), an exotic magnetic state with strongly fluctuating and highly entangled spins down to zero temperature, is a main theme in current condensed matter physics. However, there is no smoking gun evidence for deconfined spinons in any QSL candidate so far. The disorders and competing exchange interactions may prevent the formation of an ideal QSL state on frustrated spin lattices. Here we report comprehensive and systematic measurements of the magnetic susceptibility, ultralow-temperature specific heat, muon spin relaxation (µSR), nuclear magnetic resonance (NMR), and thermal conductivity for NaYbSe<sub>2</sub> single crystals, in which Yb<sup>3+</sup> ions with effective spin-1/2 form a perfect triangular lattice. All these complementary techniques find no evidence of long-range magnetic order down to their respective base temperatures. Instead, specific heat, µSR, and NMR measurements suggest the coexistence of quasi-static and dynamic spins in NaYbSe<sub>2</sub>. The scattering from these quasi-static spins may cause the absence of magnetic thermal conductivity. Thus, we propose a scenario of fluctuating ferrimagnetic droplets immersed in a sea of QSL. This may be quite common on the way pursuing an ideal QSL, and provides a brand new platform to study how a QSL state survives impurities and coexists with other magnetically ordered states.

## INTRODUCTION

Quantum spin liquid (QSL) is a highly entangled quantum state in which spins remain disordered and dynamic even down to absolute zero temperature because of strong quantum fluctuations.<sup>1–6</sup> Such an exotic state was first proposed from the study of the triangular-lattice Heisenberg antiferromagnets in 1973 by Anderson.<sup>1</sup> Since QSL has potentially tight relationship with high-temperature superconductivity<sup>7</sup> and guantum information applications,<sup>8</sup> it has gained continuous attention in condensed matter physics. The QSL states are characterized by fractional spin excitations, such as spinons, and the detection of these excitations is a crucial issue for identifying QSL in real materials.<sup>2-6</sup> Several QSL candidates have been suggested by experiments, typical examples include triangular-lattice organic compounds  $\kappa$ -(BEDT-TTF)<sub>2</sub>Cu<sub>2</sub>(CN)<sub>3</sub><sup>9-11</sup> and EtMe<sub>3</sub>Sb  $[Pd(dmit)_2]_2$ , <sup>12-14</sup> kagome-lattice ZnCu<sub>3</sub>(OH)<sub>6</sub>Cl<sub>2</sub>, <sup>15-19</sup> honeycomb lattice  $\alpha$ -RuCl<sub>3</sub>,<sup>20–23</sup> and H<sub>3</sub>Lilr<sub>2</sub>O<sub>6</sub>.<sup>24</sup> Despite numerous efforts made in both theoretical and experimental sides, finding realistic smoking gun evidence for QSLs remains the most challenging task in this field. One of the obstacles comes from the ambiguous role played by the impurities and competing exchange interactions: are they fatal or vital to the survival of a QSL?

In recent few years, the inorganic compound YbMgGaO<sub>4</sub>, in which Yb<sup>3+</sup> ions with effective spin-1/2 form a perfect triangular lattice, was argued to have a QSL ground state.<sup>25–27</sup> Although muon spin relaxation (µSR) experiments are consistent with persistent spin dynamics and no static magnetism  $\geq 0.003$   $\mu_B$  per Yb ion,<sup>28,29</sup> the absence of magnetic thermal conductivity at extremely low temperature casts doubts,<sup>30</sup> and the observation of frequency-dependent peak of AC magnetic susceptibility suggests a spin-glass ground state in YbMgGaO<sub>4</sub>.<sup>31</sup> It was argued that the random occupation between Mg<sup>2+</sup> and Ga<sup>3+</sup> can induce distortions and result in a disorder of magnetism that mimics

the QSL state.<sup>32</sup> Thus, a random spin singlet state, or valence bond glass, was proposed to account for the observations.<sup>33–35</sup>

Compared with YbMgGaO<sub>4</sub>, the family of Yb dichalcogenide delafossites NaYb(O, S, Se)<sub>2</sub> with effective spin-1/2 has a simpler structure, thus is free from the Mg-Ga disorders in non-magnetic layers.<sup>36,37</sup> As shown in Figure 1A, in the structure of NaYbSe<sub>2</sub>, magnetic Yb<sup>3+</sup> ions form flat triangular layers, and each Yb<sup>3+</sup> ion has 6-fold coordination with Se atoms to form a YbSe<sub>6</sub> octahedron. Interlinked between these flat triangular layers are sheets of Na atoms, which was once believed to be a perfect frustration system to clarify whether there is a QSL ground state in clean triangular lattice of Yb<sup>3+</sup> ions. However, it was reported that approximately 5% Na sites are occupied by Yb in NaYbSe<sub>2</sub> single crystal.<sup>38</sup>

All three compounds NaYb(O, S, Se)<sub>2</sub> are free from long-range order (LRO) down to 50 mK determined from zero field (ZF) specific heat and  $\mu$ SR measurements.<sup>36–41</sup> However, including an isostructural compound CsYbSe<sub>2</sub>, all of them have field-induced magnetic orders.<sup>39,42–45</sup> Very recently, the ground state of NaYbSe<sub>2</sub> is claimed to be a QSL with spinon Fermi surface.<sup>38</sup> A similar result is also reported in NaYbSe<sub>2</sub>.<sup>46</sup> Pressure-induced superconductivity is also observed in NaYbSe<sub>2</sub>,<sup>47,48</sup> opening up a promising way to study the mechanism of superconductivity in QSL candidates.

Here we report the magnetic susceptibility, specific heat,  $\mu$ SR, nuclear magnetic resonance (NMR), and ultralow-temperature thermal conductivity measurements on NaYbSe<sub>2</sub> single crystals. The absence of magnetic order and spin glass is confirmed by different techniques down to 50 mK. With decreasing temperature in ZF, a hump followed by a linear temperature-dependent specific heat is observed. In  $\mu$ SR and NMR measurements, both quasi-static and dynamic spins are found clearly in NaYbSe<sub>2</sub>. Furthermore, the residual linear term of thermal conductivity at all fields is negligible, pointing to the absence of itinerant fermionic magnetic excitations in NaYbSe<sub>2</sub>. Our data reveal that NaYbSe<sub>2</sub> hosts a ground state of fluctuating ferrimagnetic droplets immersed in a sea of QSL on Yb<sup>3+</sup> triangular lattice.

#### RESULTS

The temperature dependences of magnetic susceptibility  $\chi$  of NaYbSe<sub>2</sub> in external magnetic field  $\mu_0H = 1$  T in two different directions are plotted in Figure 1B. The absence of magnetic phase transition is confirmed down to 2 K. There is no splitting between ZF cooling and field cooling curves of magnetic susceptibility (Figure S2A), suggesting no spin glass in the system down to 2 K. The inset of Figure 1B presents a Curie-Weiss (CW) fit with field perpendicular to the c axis. The data above 100 K can be well fitted by CW law, giving effective moment  $\mu_{eff} = 4.54 \ \mu_{B}$  and the CW temperature  $\Theta_{CW} = -49.0$  K. The value of  $\mu_{eff}$  agrees with the theoretical prediction  $4.54 \ \mu_{B}$  for trivalent Yb<sup>3+</sup> ion with J = 7/2. Similar to YbMgGa0<sub>4</sub>, <sup>25,27</sup> magnetization *M* remains unsaturated but is smaller up to 7 T at 2 K in NaYbSe<sub>2</sub> (Figure S2B). The larger absolute value of the CW temperature and smaller *M* indicate stronger anti-ferromagnetic (AFM) interactions in NaYbSe<sub>2</sub>.

The temperature dependence of specific heat of NaYbSe<sub>2</sub> in various fields ( $H \parallel c$ ) from 0.05 to 20 K are shown in Figure 1C. Consistent with magnetic

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Figure 1. Basic properties of NaYbSe<sub>2</sub> (A) The unit cell of NaYbSe<sub>2</sub>. Green spheres, Na; red spheres, Yb; blue spheres, Se. (B) The temperature dependence of magnetic susceptibility at  $\mu_0 H = 1$  T of NaYbSe<sub>2</sub>. The inset shows the fitting result of CW law at T > 100 K. (C) The temperature dependence of specific heat C at  $\mu_0 H = 0$ , 4, and 8 T. (D) The magnetic specific heat  $C_{Maq}/T$  and the calculated magnetic entropy  $S_{Maq}$  at ZF. The red dashed line is a guide to eyes to show that  $C_{Maq}/T$  is temperature independent at low temperature.

susceptibility and former reports,<sup>38,44</sup> no sharp anomaly of LRO is observed in NaYbSe<sub>2</sub> in ZF. With decreasing temperature, a broad hump of specific heat shows up, whose position shifts to a higher temperature in magnetic field. However, we do not observe the field-induced transition peak reported previously, because of the lack of the sufficiently strong field.<sup>44</sup> For the ZF data, after subtracting the contributions from phonon and nuclear Schottky anomaly (Figure S3), we obtain the magnetic contribution of specific heat  $C_{Mag}/T$  as shown in Figure 1D. We should emphasize that the broad hump is not caused by a crystal electric field (CEF) effect, since the energy gap of CEF is approxi-

mately 15 meV, which should appear above 100 K.<sup>38,49</sup> As guided by the red dashed line, the temperature-independent behavior of  $C_{Mag}/T$  below 0.25 K is consistent with a spinon Fermi surface.<sup>38</sup> By integrating  $C_{Mag}/T$ , we obtain the magnetic entropy  $S_{Mag}$ , as shown in Figure 1D. For an effective spin-1/2 system, the theoretical magnetic entropy is  $R \ln 2$ , where R is the gas constant. The residual entropy of NaYbSe<sub>2</sub> at 50 mK is only 5.2% of total entropy. Such little entropy remaining suggests low-temperature physics is dominated by quantum fluctuations rather than thermal fluctuations, indicating the existence of QSL.



Figure 2. ZF  $\mu$ SR experiment (A) Time spectra of ZF- $\mu$ SR at representative temperatures. The curves are the fittings using Equation 1. (B) Temperature dependence of fraction of quasi-static spins. (C) Temperature dependence of relaxation rate caused by quasi-static and dynamic spins  $\sigma$  (blue spheres) and  $\lambda$  (green spheres), respectively. The error bars are statistical standard deviation in A, and are determined by the least square method in (B and C).

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Figure 3. <sup>23</sup>Na NMR experiments at 4.5 T (A) NMR spectra of <sup>23</sup>Na nuclei with external field  $\mu_0 H = 4.5$  T parallel to *c*-axis. The sharp magenta peak guided by the black dashed line is the <sup>27</sup>Al peak, which is used to calibrate the magnetic field. (B) The temperature dependence of NMR linewidth derived from the spectra as described in SM. The quasi-static (blue spheres) and dynamic (green spheres) components can be easily separated. (C) The temperature dependence of the spin-lattice relaxation rate  $1/T_1$ . The error bars are determined by the least square method in (B and C).

Both  $\mu$ SR and NMR, which measure spin dynamics at different frequency ranges, are powerful tools in clarifying the static and/or dynamic nature of the magnetic ground state.  $\mu$ SR, which uses muon as a probe, is more sensitive to local magnetic field.<sup>26,50–53</sup> As shown in Figure 2A, the time spectra of muon polarization *P*(*t*) in ZF clearly indicates that LRO, which usually induces oscillations in the spectra, is absent in ZF- $\mu$ SR down to 88 mK. Similar time spectra of muon polarization *P*(*t*) has been obtained previously<sup>54</sup>; however, we find that the relaxation process of ZF- $\mu$ SR can be best described by the sum of a Kubo-Toyabe (KT) term and an exponential term:

$$P(t) = fG_{\rm KT}(\sigma, t) + (1 - f)\exp(-\lambda t), \qquad (\text{Equation 1})$$

where *f* is the fraction of the KT term. The fitting function is exactly the same as the NaYbS<sub>2</sub> case.<sup>41</sup> The KT term originates from an isotropic Gaussian distribution of randomly oriented static or quasi-static local fields, whose relaxation rate  $\sigma$  is proportional to the root-mean-square width of the distribution.<sup>50</sup> The exponential term with relaxation rate  $\lambda$  originates from dynamic spins. The successful fitting with the above function strongly suggests the coexistence of distinguishable quasi-static spins and dynamic spins.

The temperature dependence of f,  $\sigma$ , and  $\lambda$  are plotted in Figures 2B and 2C. At high temperatures, the value of f is equal to 1, indicating a trivial paramagnetic state, which is also supported by a temperature-independent NMR intensity (see Figure S7B and related discussion in Supplementary Materials). Because of the magnetic exchange interaction, with decreasing temperature

from 20 K to 6 K, the system gradually turns into a non-trivial paramagnetic state, in which spin correlation is established and significant spin dynamic appears. As a result, f decreases continuously and the second term in Equation 1 appears. Below 6 K, the temperature-dependent f stops decreasing and upturns, while the temperature-dependent  $\sigma$  also increases clearly below 6 K. These results strongly suggest the formation of guasi-static spins at low temperatures. However, both  $\sigma$  and f saturates to a finite value at low temperatures, and the saturation value of f indicates that only 23% of the sample becomes guasi-static at base temperature. In contrast, the temperature-dependent  $\lambda$ also increases below 4 K, supporting the enhancement of spin dynamics at low temperatures. The temperature-independent behavior of  $\lambda$  below 0.2 K suggests the existence of persistent spin dynamics. We would like to emphasize that these fitting parameters are fully independent and reproducible (see Figure S4 and S5 and related discussion in supplemental information.) Additional evidence for the coexistence of quasi-static and dynamic spins in NaYbSe2 comes from a longitudinal field (LF) µSR, which yields that the fluctuation rate  $\nu$  at 0.1 K is 2.8 MHz (Figure S4), larger than 1.7 MHz in NaYbS<sub>2</sub>.<sup>41</sup>

Similar evidence for the coexistence of quasi-static and dynamic spins is also found in <sup>23</sup>Na NMR experiments. As shown in Figure 3A, the three-peak structure of <sup>23</sup>Na NMR spectra at high temperature comes from quadrupole splitting of nuclei with spin number I = 3/2 (Figure 3A). With temperature decreasing, a tiny asymmetry in spectrum appears below 49 K, suggesting a new component also with three-peak structure (Figures S6A and S9), which is ascribed to the quasi-static spins as observed by our ZF-µSR measurement. As shown in

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**Figure 4.** In-plane thermal conductivity (A) The in-plane thermal conductivity of NaYbSe<sub>2</sub> in various fields ( $\mu_0 H \parallel c$ ). The solid lines are the fits to the data of 0 and 5 T below 0.4 K using Equation 2. (B) The field dependence of  $\kappa/T$  at 0.2, 0.3, and 0.4 K, respectively.

Figure 3B, the temperature dependence of full width at half-maximum shows a similar increasing behavior for these two components below 49 K, which indicates a close correlation between these two components beyond simple competition. Generally, the demagnetization effect on internal magnetic field should be taken into account for linewidth broadening. However, since the sample used in the present NMR measurements has a shape of thin flake, the demagnetization effect can be neglected in the following analysis (see details in the discussion of Figure S8). The quasi-static moment can be estimated from the broad part of NMR spectra, yielding a small value of 0.13  $\mu_{\rm B}$  (Figure S7). This result indicates that the quasi-static spins in NaYbSe<sub>2</sub> are still fluctuating, which is in sharp contrast with traditional spin glass.<sup>55,66</sup> It should be noted that, although a similar spectral broadening at a higher magnetic field, which was ascribed to a field-induced magnetic ordering, has been observed in previous NMR work on



Figure 5. Magnetic droplets immersed in a sea of QSL Each droplet has an up-up-down and Q = (1/3, 1/3) ferrimagnetic structure.

NaYbSe<sub>2</sub><sup>44</sup> and NaYbO<sub>2</sub>,<sup>42</sup> the lower magnetic field used in the present work only leads to the formation of magnetic droplets instead of a uniform magnetic ordering. This is also supported by the absence of a peak-like behavior in the temperature-dependent nuclear spin-lattice relaxation rate  $1/T_1$ .

Beside the NMR spectrum, the nuclear spin-lattice relaxation also supports the coexistence of quasi-static and dynamic spins. Inhomogeneous spin dynamics are indeed observed below 2 K accompanied by the above two-component behavior in spectrum. As shown in Figure S6C, the stretching exponent  $\beta$ , which usually depicts the inhomogeneity of spin dynamics, decreases clearly below 2 K with the value well below 1. Especially at the lowest temperature of 0.25 K, there is a clear two-component behavior appearing in the recovery curve of  $T_1$  process (Figure S6B), which is beyond a single  $T_1$  fitting with stretching exponent. This is in line with the scenario proposed above with the coexistence of quasi-static and dynamic spins. Finally, the temperature dependence of the spin-lattice relaxation rate  $1/T_1$  extracted from the stretched exponential fitting is plotted in Figure 3C. The broad hump feature around 50 K is usually ascribed to the development of strong spin correlation at a low temperature or CEF effect.<sup>42</sup> The absence of magnetic order is confirmed again by the absence of any significant critical fluctuation at low temperatures. Below 2 K,  $1/T_1$  saturates to a constant, coinciding with the persistent spin dynamics observed in µSR experiments. This result also excludes the possibility of a trivial spin glass phase, suggesting a novel magnetic ground state in NaYbSe2.

To further check the existence of gapless magnetic excitations, we performed thermal conductivity measurements to probe the possible itinerant excitations. As for a QSL candidate, thermal conductivity measurement is highly advantageous in probing such elementary excitations, since it is only sensitive to itinerant excitations. In a solid, the contributions to thermal conductivity come from various quasi-particles, such as phonons, electrons, magnons, and spinons. Since NaYbSe<sub>2</sub> is an insulator, electrons do not contribute to the thermal conductivity at ultralow temperatures. Additionally, the contribution of magnons can be ruled out because of the absence of magnetic order down to 50 mK. Therefore, thermal conductivity  $\kappa$  at ultralow temperatures can be described by the formula

$$\kappa = aT + bT^{\alpha},$$
 (Equation 2)

where aT and  $bT^{\alpha}$  represent the contribution from possible itinerant gapless fermionic magnetic excitations and phonons, respectively.<sup>57,58</sup> Because of the specular reflections of phonons at the sample surfaces, the power  $\alpha$  in the second term is typically between 2 and 3.<sup>57,58</sup>

The in-plane thermal conductivity of NaYbSe<sub>2</sub> in zero and various fields ( $\mu_0 H \parallel c$ ) are shown in Figure 4. In ZF, the fitting to the data below 0.4 K gives the residual linear term  $\kappa_0/T \equiv a = -0.038 \pm 0.007$  mW K<sup>-2</sup> cm<sup>-1</sup> and  $\alpha = 1.66 \pm 0.04$ . This unusual behavior is very similar to YbMgGaO<sub>4</sub>,<sup>30</sup> both in the unphysical negative  $\kappa_0/T$  and abnormally low value of  $\alpha$  ( $\kappa_0/T = -0.025 \pm 0.002$  mW K<sup>-2</sup> cm<sup>-1</sup> and  $\alpha = 1.85 \pm 0.04$  for YbMgGaO<sub>4</sub>).<sup>30</sup> For comparison, we also measured the thermal conductivity of the non-





Figure 6. Spinon Fermi surfaces and gauge fluxes in the theoretical model (A) Spinon Fermi surfaces. Black hexagon denotes the first Brillouin zone. Red and blue triangles are Fermi surfaces for spin up and down spinons, respectively, where the flux is chosen to be  $\Phi = \pi/2$ . The arrow indicates the nesting wave vector Q = (1/3, 1/3). (B) Staggered gauge fluxes.

magnetic NaLuSe<sub>2</sub> single crystal, as plotted in Figure S10. There is no magnetic field effect on the thermal conductivity of NaLuSe2, and its thermal conductivity shows a typical phonon behavior in the boundary scattering limit, with  $\kappa_0/T = -0.008 \pm 0.010$  mW K<sup>-2</sup> cm<sup>-1</sup> and  $\alpha = 2.57 \pm 0.05$ . More important, the magnitude of thermal conductivity for NaYbSe<sub>2</sub> is lower than that of NaLuSe<sub>2</sub>. Again, this is a similar situation to YbMgGaO<sub>4</sub>, which has a lower magnitude than non-magnetic LuMgGaO4.30 We note that the magnitude of  $\kappa/T$  is comparable between NaYbSe<sub>2</sub> and YbMgGaO<sub>4</sub> in ZF. Previously, we estimated the upper limit of the spinon (if it exists) means a free path in YbMgGaO<sub>4</sub> is 8.6 Å, approximately 2.5 times that of the interspin distance.<sup>30</sup> Considering the comparable  $\kappa/T$  and similar triangular Yb lattice, the spinon mean free path in NaYbSe<sub>2</sub> should also be no more than 10 Å. In Figure 4A, the fitting to the data of  $\mu_0 H = 5$  T gives  $\kappa_0 / T = -0.041 \pm$ 0.001 mW K<sup>-2</sup> cm<sup>-1</sup> and  $\alpha$  = 1.97 ± 0.05. Therefore,  $\kappa_0/T$  is virtually zero in all fields, indicating the absence of itinerant gapless magnetic excitations in NaYbSe<sub>2</sub>, and its thermal conductivity is mainly contributed by phonons. Figure 4B plots the field dependence of the  $\kappa/T$  at 0.2, 0.3, and 0.4 K. For  $\mu_0 H$ < 3 T,  $\kappa/T$  is independent of fields. With increasing fields, the spins are increasingly polarized, thus reducing the scattering of phonon, leading to the rapid enhancement of thermal conductivity from 3 to 5 T, as observed in YbMgGaO<sub>4</sub>.30

### DISCUSSION

We now turn to discuss the ground state of NaYbSe<sub>2</sub>. The absence of LRO and spin glass in NaYbSe<sub>2</sub> is confirmed down to 50 mK. Both  $\mu$ SR and NMR experiments point out that a minority of quasi-static spins and a majority of dynamic spins co-exist in NaYbSe<sub>2</sub> down to the base temperature. In fact, our specific heat measurements also hint at this picture. The broad hump of  $C_{Mag}/T$  at approximately 0.8 K comes from the correlations of quasi-static spins, while the temperature-independent behavior below 0.25 K suggests the existence of well-defined magnetic excitations, which is an essential feature of gapless QSLs.<sup>24,38,39</sup> Comparing our results in ZF, these two characteristic temperatures coincide with our µSR data astonishingly. We note that the external field applied in the NMR experiments could affect the ground state, and the experimental principles of NMR and µSR are different, so the results of NMR cannot be compared with  $\mu$ SR or specific heat directly. As for the thermal conductivity measurements, the dynamic spins should result in a finite residual linear term  $\kappa_0/$ T in NaYbSe<sub>2</sub>.<sup>59-61</sup> However, the gapless spinons may be strongly scattered by the quasi-static spins, leading to a negligible  $\kappa_0/T$ .

We propose here a possible picture of a mixed state of fluctuating short-range up-up-down ferrimagnetic droplets and QSL. As for the minority quasi-static

spins, there are no long-range but at least short-range correlations between them. Since there is AFM interaction on a triangular lattice, the total moment cannot be canceled. Therefore, we take the state as an up-up-down ferrimagnetic state. They are not static like spin glass, and our NMR result suggests that they are still fluctuating. They only take 23% of the total spins, suggesting they distribute in the system like droplets. Such droplets might come from the 5% wrong occupation at Na sites, which is difficult to avoid.<sup>38</sup> Note that such 5% site-mixing (Na-Yb) ratio is obtained by single-crystal X-ray refinements, while the powder neutron scattering refinement suggests an upper limit of 10% of Yb at the Na site.<sup>38</sup> From our powder X-ray refinements (data not shown), this ratio is approximately 11.6%. When it comes to the dynamic spins, they remain disordered and fluctuating down to our base temperature, exactly matching the definition of QSL. The evidence for spinon Fermi surface was also given by our specific heat measurements. Additionally, there is only < 5.2% residual entropy at zero temperature, also indicating the presence of QSL. The same scenario was also proposed for NaYbS<sub>2</sub>.<sup>41</sup>

Now it brings us to why other methods like magnetic susceptibility and neutron scattering do not observe such ferrimagnetic droplets.<sup>36,38</sup> For the magnetic susceptibility technique, it is more sensitive to slower fluctuations, whose limit is about 10<sup>4</sup> Hz, while NMR and  $\mu$ SR are more sensitive to faster fluctuations. Hence a state could be dynamic in magnetic susceptibility measurements, but quasi-static in NMR and  $\mu$ SR. In inelastic neutron scattering experiments, such fluctuating droplets could also mimic spinon continuum because of its randomness, making it difficult to differentiate.

The ferrimagnetic droplets immersed in a sea of QSL are illustrated in Figure 5, on which an up-up-down magnetic structure forms within each droplet in accordance with field-induced AFM orders in Yb<sup>3+</sup> compounds on triangular lattice.<sup>39,42–45</sup> It is natural to assume that such a ferrimagnetic ordering state has a slightly higher energy than the QSL state, which allows the nucleation of ferrimagnetic droplet around a defect. Meanwhile, the thermal fluctuation of these magnetic droplets will give rise to the residual entropy. The ratio between the residual entropy and the total magnetic entropy is estimated to be  $\frac{rln(1+m/3)}{mn2}$ , where *r* is the volume fraction of droplets and each droplet carries *m* Yb<sup>3+</sup> ions. It is expected that the size of the fluctuating droplets will be enhanced by an external magnetic field, resulting in a long-ranged AFM order in bulk when the applied magnetic field exceeds some threshold.<sup>39,42–45</sup>

Other remaining issues include why an impurity favors a  $\mathbf{Q} = (1/3, 1/3)$  magnetic droplet in such a QSL and what kind of QSLs can host this possibility. These issues can be addressed by assuming a nested (or nearly nested) spinon Fermi surface as illustrated in Figure 6A, which indicates the instability of the spinon Fermi surface. Thus, a spinon density wave, that is, a magnetic ordered structure of the wave vector  $\mathbf{Q} = (1/3, 1/3)$  will be energetically favored. An impurity in a

QSL background can be viewed as a hole of local magnetic moments. It will generate a Ruderman-Kittel-Kasuya-Yosida-like (RKKY) oscillation that is characterized by the spin susceptibility function  $\chi(\mathbf{q}, \omega = 0)$ , provided that there exists a spinon Fermi surface. If the spinon Fermi surface becomes nested, the spin susceptibility  $\chi(\mathbf{q}, \omega = 0)$  will diverge at the nesting wave vector  $\mathbf{q} = \mathbf{Q}$ , resulting in a magnetic ordering in short range, so that the nucleation of a  $\mathbf{Q} = (1/3, 1/3)$  magnetic droplet comes into being around the impurity.

However, an usual spin rotationally invariant system, such a nested Fermi surface, leads to a 1/3-filling spinon band instead of the 1/2-filling spinon band (see Figure 6A) required by the Mottness. This seeming contradiction can be resolved by considering the spin-orbit interaction that comes from the buckling of Se atoms and spoils the spin rotational symmetry. Because of the buckling, triangular layers YbSe<sub>6</sub> has a  $D_{3d} = D_3 \times I = C_{3v} \times I$ , but not  $C_6$  rotational symmetry. To solve the problem, we consider an effective Hamiltonian as follows,

$$H_{\rm eff} = -t \sum_{(mn),s} e^{is\theta_{mn}} c^{\dagger}_{ms} c_{ns}, \qquad (\text{Equation 3})$$

where (mn) denotes a pair of nearest neighbor sites m and n on a triangular lattice,  $c_{ms}^{\dagger}$  creates a fermionic spinon,  $s = \pm 1$  refers to up (down) spin (or to be precise, pseudospin), and  $\theta_{mn}$  are phases that give rise to staggered gauge fluxes  $\pm \Phi$  on elementary triangles (see Figure 6B). Note that both  $C_{3\nu}$ and the time-reversal symmetry are respected by the Hamiltonian  $H_{\rm eff}$ , because the net gauge flux through a unit cell (containing two triangles) is zero. However, the spatial inversion symmetry *I* is been broken. When  $\Phi = 0$ , the spin-rotational symmetry is restored, together with the spatial inversion symmetry, yielding in a circle spinon Fermi surface at 1/2-filling. When  $\Phi \neq 0$ , up and down spinons possess two different Fermi surfaces at 1/2-filling. These two Fermi surfaces can be transformed to each other under a time-reversal or a reflection. In particular, when  $\Phi = \pi/2$  (or  $-\pi/2$ ), as illustrated in Figure 6A, the two spinon Fermi surfaces become two perfect triangles, and their edges are nested by a wave vector  $\mathbf{Q} = (1/3, 1/3)$  or its  $C_3$  rotations. Therefore, we suggest that the QSL depicted by the effective Hamiltonian  $H_{eff}$  in Equation 3 is a promising candidate for the paramagnetic phase bordering a Q = (1/3, 1/3) magnetic ordering state in NaYbSe<sub>2</sub>. The QSL to magnetic ordering phase transition occurs at  $\Phi = \pm \pi/2$ .

## CONCLUSION

We present specific heat,  $\mu$ SR, NMR, and thermal conductivity measurements on triangular-lattice compound NaYbSe<sub>2</sub> single crystals to figure out its ground state. The absence of long-range magnetic order and spin glass is confirmed down to 50 mK. Specific heat,  $\mu$ SR, and NMR measurements all find a majority of dynamic spins and a minority of quasi-static spins mixed in NaYbSe<sub>2</sub>, which is further supported by thermal conductivity measurements. The ground state of NaYbSe<sub>2</sub> can be regarded as a mixed state with both QSL and fluctuating short-range ferrimagnetic droplets, providing a platform to study how disorder influences the QSL state.

# MATERIALS AND METHODS Sample preparation

High-quality NaYbSe<sub>2</sub> single crystals were grown by a modified flux method following Schleid and Lissner.<sup>62</sup> Analytically pure Yb powder, Se powder, and NaCl as flux in a molar ratio of 2:3:90 were sealed in a quartz tube and heated to 950°C for 7 days, followed by a maintaining at 950°C for 7 days. The mixture was slowly cooled down to 600°C at a rate of 50°C per day. In the end, reddish-black platelets with largest size of 7–8 mm, as shown in the inset of Figure S1, were separated by dipping in water. The large natural surface was determined to be the (001) plane by X-ray diffraction, as illustrated in Figure S1 and no impurity phases were observed, indicating a relatively high crystallization quality.

#### **Magnetic measurements**

The magnetic susceptibility measurements were performed in commercial SQUID and the specific heat was measured in the physical property measurement system (PPMS, Quantum Design) by the relaxation method.

#### **µSR measurements**

In a  $\mu$ SR experiment, a beam of nearly 100% spin polarized muon is implanted into the sample. Muon spin precesses and relaxes because of an inhomogeneous local magnetic

field. One can measure the time spectra of muon spin polarization, and the relaxation process can reveal the distribution of local field.<sup>28,51,52</sup> Besides, muon is extremely sensitive to small field, which is a powerful technique to check the essence of magnetic order.<sup>53</sup> ZF and LF  $\mu$ SR measurements were performed down to 88 mK on MuSR spectrometer at ISIS, Rutherford Appleton Laboratory, Chilton, UK. Single crystals of NaYbSe<sub>2</sub> are aligned so that the *c* axis is normal to the sample's planar surface and parallel to the initial muon spin polarization and mounted onto a silver holder covering a circle area of 1 inch in diameter and 3 mm in thickness.  $\mu$ SR data were analyzed using the MANTID PROJECT and MUSRFIT software packages.<sup>63</sup> Subtracting the constant background signal due to silver sample holder, ZF muon spin polarization spectra *P*(*t*) can be described by the formula *P*(*t*) =  $fG_{KT}(\sigma, t) + (1 - f)\exp(-\lambda t)$ , where  $G_{KT}(\sigma, t) = \frac{1}{3} + \frac{2}{3}(1 - \sigma^2 t^2)\exp(-\frac{1}{2}\sigma^2 t^2)$  is the KT function.<sup>50</sup>

#### NMR measurements

The <sup>23</sup>Na NMR measurements are taken on one piece of NaYbSe<sub>2</sub> single crystal with the mass of 2.6 mg. Because the nuclear gyromagnetic ratios for <sup>23</sup>Na ( $\gamma_{Na}$  = 11.2625 MHz/T) is very close to <sup>63</sup>Cu ( $\gamma_{Cu}$  = 11.285 MHz/T), we chose the Ag wire to wind NMR coil. To define the exact external magnetic field, we fill a small piece of Al foil into the coil. The NMR spectra are obtained by the fast Fourier transformation sum of the standard spin-echo signals. The linewidth is extracted from Gaussian fitting. Especially when fitting the spectra of dynamic part between 0.25 K and 1.5 K, we fixed the linewidth of the central line and the satellite line to be the same. The nuclear spin-lattice relaxation rate  $1/T_1$  is measured by saturation method below 1.5 K and inverse method for higher temperature. The recovery curve of the nuclear magnetization M(t) is fitted with the function  $1 - \frac{M(t)}{M(\infty)} = I_0 \left\{ 0.1 \exp\left[ - \left(\frac{t}{T_1}\right)^{\beta} \right] + 0.9 \exp\left[ - \left(\frac{6t}{T_1}\right)^{\beta} \right] \right\}$ . The error bars are determined by the least squares method.

#### Thermal conductivity measurements

The single crystal selected for the thermal conductivity measurements was a rectangular shape of dimensions  $5.38 \times 1.30 \text{ mm}^2$  in the *ab* plane, with a thickness of 0.04 mm along the *c* axis. The thermal conductivity was measured in a dilution refrigerator, using a standard four-wire steady-state method with two RuO<sub>2</sub> chip thermometers, calibrated *in situ* against a reference RuO<sub>2</sub> thermometer. Magnetic fields were applied along the *c* axis for specific heat and thermal conductivity measurements and perpendicular to the heat current in the thermal conductivity measurements.

#### **Residual entropy**

Assuming each ferrimagnetic droplet carries *m* spin-1/2 ( $J_{eff} = 1/2$  local moment) and the fractional volume of the ferrimagnetic droplets is *r*, then the effective spin of each droplet is  $\overline{S} = \frac{m}{3} \times \frac{1}{2}$ , which gives rise to the upper bound of the residual entropy  $R\ln(1 + 2\overline{S}) = R\ln(1 + m/3)$ . Thus, the ratio between the residual entropy and the total magnetic entropy at high temperatures has an upper bound of  $\frac{r\ln(1+m/3)}{mn^2}$ .

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# **AUTHOR CONTRIBUTIONS**

L.S. and S.L. planned the project. B.P. synthesized the sample, and characterized the sample with C.J. Z.Z., Y.Yang, and C.C. carried out the  $\mu$ SR experiments with experimental assistance from A.D.H. L.N. carried out the NMR experiments. B.P., J.N., Y.H., E.C., and Y.Yu performed the thermal conductivity measurements. L.S., S.L., T.W., Z.Z., B.P., L.N., and J.N. analyzed the data. Y.Z. and J.M. provided the theoretical explanation. L.S., S.L., T.W., Y.Z., X.C., Z.Z., B.P., and L.N. wrote the paper.

# **DECLARATION OF INTERESTS**

The authors declare no competing interests.

# DATA AVAILABILITY

All data needed to evaluate the conclusions in the paper are present in the main text or the supplemental information.

# SUPPLEMENTAL INFORMATION

It can be found online at https://doi.org/10.1016/j.xinn.2023.100459.

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