Extracting stellar emissivity via a machine learning analysis of MSX and LAMOST catalog data

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Many astronomical studies model stars like radiating blackbodies with unit emissivity. Their conclusions should be reconsidered if the stellar spectral emissivity, \( \varepsilon_\lambda \), were to be proven to be appreciably smaller. However, determining \( \varepsilon_\lambda \) from raw observational data poses serious technical challenges. Here, using a machine learning technique, we implemented an inverse model for calculating the stellar spectral radiation flux in a given spectral band emissivity. Radiation flux data in some spectral bands serve as input to determine the unknown model parameters. To this purpose, we chose 411 stars (361 from the Midcourse Space Experiment (MSX) catalog and 50 from the Large Sky Area Multi-Object Fiber Spectroscopic Telescope (LAMOST) catalog) as training samples of a stochastic particle swarm optimization algorithm. The mean values of the emissivity estimates thus obtained deviate significantly from the ideal blackbody value. Knowledge of the model parameters then enabled us to calculate the radiation fluxes in other spectral bands to compare with the existing observational data and thus validate our approach. Finally, based on the trained algorithm, we discuss our predictions for spectral bands where astronomical data are unavailable. Besides providing direct evidence against modeling stars as emitting blackbodies, our conclusions also call for more direct investigations of the stellar emissivity.

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I. INTRODUCTION

Determining the star age is key to understanding the origin of the Universe [1]. The first step to determining it is to classify the observed star based on its spectral characteristics, say, whether it is a blue dwarf with an abnormally strong internal nuclear fusion reaction or a yellow dwarf with a moderate reaction intensity or, perhaps, an orange or red dwarf with a low reaction intensity [2]. Moreover, the spectral analysis of the radiation from the star can reveal valuable information about its effective temperature, atmosphere, ionization state, surface gravity, rotation rate, and the abundance of elements [3]. In this regard, we remind the reader that the wide spectral range of the James Webb Space Telescope, spanning from visible to near-(0.6–5.3 \( \mu \)m) and midinfrared (5–28 \( \mu \)m) [4–7], was specifically designed to allow high-precision measurements of star ages. A related observable essential in the study of stellar evolution is the radiation flux, which depends on the star luminosity and its distance from the Earth [8–12]. The observation of radiation fluxes in different spectral emission bands [13] provides additional information about celestial bodies.

One can estimate the radiation flux from a star by using models for the stellar effective temperature, band emissivity, and the detection angular parameter [14,15]. Stellar emissivity is the ratio of the radiation emitted by a star surface to the radiation emitted by a blackbody at the same wavelength. Thus, it ranges from 0 to 1 [16–20]. In fact, stars are not perfect blackbodies, and their emissivity is not the same across the entire emission spectrum [21–25]. The radiation fluxes measured by a detector may not conform to Planck’s law predictions because of the wavelength
dependence of the stellar emission and/or absorption processes [26]. Most of such processes takes place in the star atmosphere, which, in turn, is characterized by variable patterns of temperature, pressure, density, and element abundance [27]. Consequently, the relevant radiation flux cannot be accurately estimated if the star emissivity is conventionally set to 1 [28,29]. Indeed, the emissivity of a star should be evaluated together with its effective temperature to mitigate systematic errors in the estimates of the radiation fluxes [30,31]. On the other hand, determining the stellar spectral emissivity from raw observational data proved to be a challenging task, hence the often unwarranted assumption of stars as blackbody emitters.

The stellar effective temperature is a relatively well-investigated parameter due to its significance in the current theories of stellar evolution. One can estimate it by having recourse to different methods, namely, the direct measurement method [32–35], the infrared flux method [36–39], and the template matching method [40–42]. Contrary to the stellar effective temperature, there is no well-established method to extract reliable estimates of the stellar spectral emissivity from the available observational data. On the other hand, as anticipated above, assuming ideal emissivity \( \varepsilon_\lambda = 1 \) at all wavelengths may lead to unwanted inaccuracies in the determination of the radiation fluxes.

To address this problem, we propose a machine learning technique to train an inverse model for the radiation flux of a star of assigned spectral emissivity and effective temperature, i.e., with atmosphere thick enough for its surface to be in thermodynamic equilibrium [43]. In a previous study [44], a similar technique was applied to investigate the much simpler problem of the total radiation flux dependence on the effective temperature, alone. We implement a stochastic particle swarm optimization algorithm to determine the model parameters (spectral emissivity, effective temperatures, and detection angular parameters) in select spectral bands for a number of reference stars. The resulting mean emissivity values are confirmed to deviate significantly from the ideal blackbody value. After training, the model can be successfully employed to predict the radiation fluxes in other spectral bands and compare them with the existing observational data when available.

**II. METHODS**

**A. Model of stellar radiation fluxes**

Stellar radiation fluxes are usually extracted from the survey data of astronomical telescopes within specified spectral bands. The fluxes from a star detected on Earth may depend on many factors, including its temperature, the interstellar dust, and the star-detector distance. To simplify data analysis, we assume, as customary in the literature, stellar radiation fluxes to be a heuristic function of three effective stellar parameters only: namely, the band emissivity, the surface temperature, and the detection angular parameter. Sufficiently accurate knowledge of these three quantities yields reliable estimates of the relevant stellar radiation fluxes.

The spectral radiation flux in the wavelength band \((\lambda_i, \lambda_i + \Delta\lambda_i)\) from a blackbody at temperature \(T\) is described by Planck’s law [45]

\[
E_{\lambda_{ij}} = \frac{c_1 \lambda_i^{-5}}{\exp(c_2/(\lambda_i T)) - 1} \Delta\lambda_i
\]

where \(c_1\) and \(c_2\) are the first and second radiation constants, respectively. The corresponding band radiation flux from a star can be expressed as \(E_{\lambda_i} = \varepsilon_{\lambda_i} E_{\lambda_{ij}}\), where \(\varepsilon_{\lambda_i}\) is the relevant star band emissivity. Recalling that the band radiation intensity is \(I_{\lambda_i} = E_{\lambda_i}/\pi\) and the stellar detection solid angle is \(d\Omega = \pi r^2/R^2\) (see Fig. 1), then, the band radiation flux on the detector can be rewritten as \(E_{p\lambda_i} = I_{\lambda_i} d\Omega\); that is

\[
E_{p\lambda_i} = \varepsilon_{\lambda_i} \xi \int_{\lambda_i}^{\lambda_i + \Delta\lambda_i} \frac{c_1 \lambda_i^{-5}}{\exp(c_2/(\lambda_i T)) - 1} d\lambda_i
\]

where \(r\) is the stellar radius, \(R\) is the star-detector distance, and

\[
\xi = r^2/R^2
\]

is the detection angular parameter.

In conclusion, \(E_{p\lambda_i}\) is expressed as a relatively simple function of three parameters, the band emissivity \(\varepsilon_{\lambda_i}\), the
stellar effective temperature $T$, and the detection angular parameter $\xi$, i.e.,

$$E_{\lambda i} = f(e_{\lambda i}, T, \xi),$$

which defines the forward problem numerically addressed in this work.

**B. Inverse problem**

The difficulty of the problem is that the stellar radiation fluxes are known for several emission bands, but the model parameters, including the stellar effective temperature and band emissivity, are not. The model parameters need then to be extracted self-consistently from the known radiation fluxes. For this purpose, we developed a machine learning algorithm to solve the relevant inverse problem. The equations to solve can be formulated as

$$e_{\lambda i}, T, \xi = \mathcal{F}(E_{\lambda i}),$$

where the band index $i$ runs from 1 to 3. We agreed to solve the inverse problem for the radiation fluxes in three specific wavelength bands of the Midcourse Space Experiment (MSX) catalog, namely, 6.8–10.8, 4.24–4.45, and 13.5–15.9 $\mu$m, respectively [46]. In the MSX catalog, infrared flux densities are reported for six wavelength bands between 4.2 and 25.1 $\mu$m [47]. Estimates of the right ascension, declination, and proper motion are also listed in the catalog. The flux densities of radio sources are defined as the emitted energy per unit frequency interval, unit area, and unit time interval [48–51]. The flux density unit adopted in the catalog is Jy [52], which can be converted to the corresponding SI unit as

$$1 \text{ Jy} = 10^{-26} \text{ W/(m}^2 \cdot \text{Hz)}.$$  

The radiation fluxes can be calculated by integrating the average energy density over the band [53], namely,

$$E_{\lambda 1-\lambda 2} = \int_{\lambda 1}^{\lambda 2} E_{\lambda i} d\lambda,$$

where $E_{\lambda i}$ denotes the radiation flux in the relevant wavelength interval or band.

For the three-band inverse problem, there are five unknown variables (stellar effective temperature, detection angular parameter, and three values of band emissivity), so Eq. (5) admits infinite solutions.

To numerically attack the problem, each emission band was divided into about 100 intervals. The stellar emissivity was assumed to be not far from 1.00 because stellar spectra are known to not differ much from blackbody spectra [28,29]. Eventually, the most appropriate variability range for the stellar band emissivity was narrowed down to (0.90,1.00). The effective temperature and detection angular parameter were computed for different values of the star emissivity. The choice corresponding to the minimum value of an adaptive parameter (the best fitness) was taken as the optimal final choice.

The deviation $\Delta T_{\text{eff}}$ of the stellar effective temperatures reported in the literature $T_{\text{eff}}^{\text{ref}}$ from the values $T_{\text{eff}}^{\text{present}}$ estimated in this work is defined as

$$\Delta T_{\text{eff}} = T_{\text{eff}}^{\text{ref}} - T_{\text{eff}}^{\text{present}}.$$  

The radiation fluxes corresponding to different detection bands are then calculated by using the estimated values of the band emissivity, stellar effective temperature, and detection angular parameter. Accordingly, the relative error $\delta$ associated with the calculated radiation fluxes is

$$\delta = (|E_c - E_m|/E_m) \times 100\%,$$

where $E_c$ and $E_m$ are, respectively, the radiation fluxes calculated through our technique and those reported in the telescope observational catalog.

**C. Algorithm selection**

The stochastic particle swarm optimization (SPSO) algorithm was designed to solve the inverse problem. The key idea is that the potential solutions are represented by particles moving in the solution space with a certain velocity. The optimal solution is determined by monitoring an adaptive parameter, the fitness, which quantifies how close the solution is to an objective value. The search space of $D$ dimensionality is populated by $M$ particles of coordinates $X_i = (x_{i1}, x_{i2}, \ldots, x_{iD})$, and velocity is populated by $V_i = (v_{i1}, v_{i2}, \ldots, v_{iD})$, with $i = 1, 2, \ldots M$. The best position experienced at a given time $t$ by the $i$th particle is denoted by $P_i = (p_{i1}, p_{i2}, \ldots, p_{iD})$; the absolute best position among all $M$ particles at the same time is $P_g = (p_{g1}, p_{g2}, \ldots, p_{gD})$.

The velocity $V_i$ of each particle is given in terms of local and global values [54,55],

$$V_i(t+1) = wV_i(t) + c_1 r_1 (P_i(t) - X_i(t)) + c_2 r_2 (P_g(t) - X_i(t)).$$

Here, $i$ is the iteration time, $w$ is the inertia weight, $c_1$ and $c_2$ are acceleration constants, and $r_1$ and $r_2$ are random numbers in the interval $[0, 1]$. Then, the new position $X_i$ of the particle is determined by

$$X_i(t+1) = X_i(t) + V_i(t+1).$$
In our computations, we set the algorithm parameters as follows: number of particles \( M = 50 \); maximum number of iteration \( t = 10,000 \); inertia weight \( w = 0.0 \); acceleration constants \( c_1 = 1.80 \) and \( c_2 = 1.80 \); and space dimensions equal the number of variables in the problem, \( D = 3 \). The expected solution ranges are 1000–20,000 K for the effective temperatures, \( 1.0 \times 10^{-21}–1.0 \times 10^{-16} \) for the detection angular parameters, and 0.90–1.00 for the band emissivity values. However, the above ranges have been expanded to meet the computing requirements, namely, \( 1.0 \times 10^{-25}–1.0 \times 10^{-5} \) K for the effective temperatures, \( 1.0 \times 10^{-26}–1.0 \times 10^{-10} \) for the detection angular parameter, and 0.90–1.00 for the band emissivity values. These latter ranges determine the boundaries of the particle swarm space.

D. Algorithm details

1. Effects of the number of particles on convergence

The number of particles \( M \) in the SPSO algorithm has a direct impact on the inversion efficiency and therefore on the output accuracy. Thus, one needs to determine an optimal choice for \( M \). There are two algorithm “end” criteria: (1) the iteration accuracy is below a fixed level of \( 10^{-10} \), and (2) the iteration number (or time) is larger than 10,000.

The convergence trends for different \( M \) values (10, 20, 50, 70, and 100) were compared to choose the optimal particle number. The best fitness values characterize the convergence trends as a function of the iteration time as shown in Fig. 3(a).

The best fitness decreases with the growth of iteration time until it hits the minimum value \( 1.37 \times 10^{-5} \). For \( M = 10 \), the convergence is the slowest. Convergence is reached after 1601 iterations for \( M = 10 \) and 501 for \( M = 20 \) and 301 for the remaining \( M \) values. The convergence trend is the most natural benchmark to choose the optimal value of \( M \); however, the code running times should also be considered for practical purposes. Figure 3(b) shows the algorithm running times for \( M = 10, 20, 50, 70, \) and 100. All the calculations were performed on a 2.80 GHz Intel Core i7-7700HQ processor. The running time grows with increasing \( M \), from 62 min for \( M = 10 \) to 636 min for \( M = 100 \).

In conclusion, when computing the model parameters, increasing \( M \) significantly increases the computation time without appreciably lowering the best fitness. Therefore, taking into account both factors, computation times and accuracy, we set \( M = 50 \) (for which the running time is 331 min).

2. Effects of the band emissivity on convergence

Figure 3(c) shows the best fitness as a function of iteration time with different band emissivity values, 0.90, 0.93, 0.95, 0.97, and 1.00.

![Flow diagram of SPSO algorithm](image-url)
All the corresponding best fitness curves decay with the iteration time and reach their minimum after 301 iterations. In particular, the best fitness minima are $1.04 \times 10^{-8}$ and $8.46 \times 10^{-9}$ for emissivity equal, respectively, to 0.90 and 0.93 and $3.38 \times 10^{-9}$ for all other emissivity values. In any case, the minimum value of the best fitness is no larger than $1.00 \times 10^{-8}$ for an appropriately high number of iterations. This proves that our algorithm can be used to determine the inverse problem parameters in the full emissivity range considered in this work.

### 3. Effects of band flux uncertainties on convergence

To assess the stability of our inverse problem solution against the uncertainty of the input data, we generated random deviations to the catalog band-flux data [56]. The actual, $Y_{\text{exact}}$, and the modified values of the band flux, $Y_{\text{est}}$, have been related as

$$Y_{\text{est}} = Y_{\text{exact}} + \sigma \cdot \eta,$$

where $\eta$ is a normally distributed random variable with mean value 0 and standard deviation 1. For a measured error $\gamma$ at 99% confidence, the standard deviation $\sigma$ of the measured flux is

$$\sigma = (Y_{\text{exact}} \cdot \gamma \%) / 2.576.$$

The relative error $\delta_{\text{rel}}$ of the estimated flux versus the exact one is
The relevant variables are the effective temperature, the detection angular parameter, and the emissivity. Moreover, the emissivity is a spectral function that yields distinct values for the different bands. Therefore, the number of unknowns is larger than the number of equations to solve. To circumvent this difficulty, we compared results from a variety of different input combinations, as reported below.

We ran our SPSO algorithm with initial effective temperature of 5000 K, detection angular parameter $2.0 \times 10^{-19}$, and emissivity 1.00. Figure 4(a) illustrates the convergence of the algorithm for different numbers of the bands available on the MSX catalog. The convergence quantifier adopted here is the best fitness parameter defined by Eq. (12). All curves on display quickly converge with increasing of the number of iterations. More remarkably, the minimum best fitness value is achieved for three bands. For this reason, we finally opted to numerically solve the inverse problem at hand by using the observational data from three spectral bands.

B. Selection of band combinations

The next question to address is how to select the most appropriate spectral bands for our analysis. As the MSX provides data for six bands and we only need three of them, we can choose from 20 combinations. Results from six band groups have been compared in detail for best algorithm performance, namely, group A (band 1, band 2, and band 3), group B (band 1, band 3, and band 5), group C (band 1, band 3, and band 6), group D (band 1, band 5, and band 6), group E (band 2, band 3, and band 4), and group F (band 4, band 5, and band 6).

The algorithm was run for each band combination and different preset flux output errors. Figure 4(b) compares the solution’s best fitness at increasing output errors for the six band groups. Group B exhibits the most stable value of the best fitness. The best fitness of group A is higher than group B for errors larger than 0.06, and so is the best fitness of group C but for errors smaller than 0.10. Finally, the best fitness of groups D, E, and F are all systematically larger than group B. Thus, group B (band 1, band 3, and band 5) was selected as our best choice for the SPSO solution of the inverse radiation flux problem.

C. Comparison of stellar effective temperature

Having tested the performance of our SPSO algorithms, we calculate now the stellar effective temperatures $T_{\text{eff}}$ and compare our results with the corresponding reference values $T_{\text{ref}}$ reported in the literature [57–60].

The upper panel of Fig. 4(c) shows a comparison between $T_{\text{eff}}$ and $T_{\text{ref}}$ for a sample of 90 stars, each represented by a blue circle [57–60]. The estimated effective temperatures span the relatively wide range 3500–6600 K. The representative points are concentrated around the solid black (diagonal) line, with most of them lying in the gray shaded area. This means that our relative
error on the effective temperatures of most stars is less than
15%; that is, the calculated temperatures are consistent with
the existing data.

The deviations \( \Delta T_{\text{eff}} \) between reference, \( T_{\text{ref}} \), and
estimated effective temperatures, \( T_{\text{present}} \) [see Eq. (8)], are reported in the lower panel in Fig. 4(c). The mean
values and standard deviations of \( \Delta T_{\text{eff}} \) computed over \( T_{\text{ref}} \)
Bins of 200 K are shown as red dots and bars, respectively.
The mean values of \( \Delta T_{\text{eff}} \) are smaller than 400 K, except
for \( T_{\text{ref}} = 5500 \text{ K} \) (500 K) and 4700 K (417 K). The
standard deviations of \( \Delta T_{\text{eff}} \) range between 301 and 912 K,
respectively, at \( T_{\text{ref}} = 6300 \text{ and } 5500 \text{ K} \). This confirms the
dependability of our numerical results for the stellar
effective temperatures.

D. Determination of stellar band emissivity

The spectral emissivity in bands 1, 3, and 5 can be
obtained by the same token, as illustrated by the correspond-
ing histograms of Figs. 5(a)–5(c). The emissivity of the
sampled stars in the three bands shows distinct qualitative
behaviors: limited to the narrow range 0.95–1.00 in band 1,
centered around 0.90 in band 5, and broadly distributed
between 0.90 and 1.00 in band 3.

The emissivity of the sampled stars in bands 1, 3 and 5
have mean, 0.98, 0.92, and 0.95, and standard deviation,
0.0161, 0.0336, and 0.0212, respectively, as displayed in
Fig. 5(d). As anticipated, the emissivity data of band 3 are
more dispersed. The values of the spectral emissivity
illustrated here, combined with the estimates of the effective
temperatures reported above, allow a self-consistent
calculation of the spectral radiation fluxes from the sampled
stars (listed in the supplemental material, Table S1 [61]).

E. Calculation of stellar radiation fluxes
in other bands with observational data

So far, data on the stellar radiation fluxes in bands 1, 3,
and 5 have been used to train the SPSO algorithm we
implemented to solve the inverse problem and thus com-
pute the unknown model parameters. Having determined
the model parameters with a satisfactory degree of con-
fidence, we can now solve the direct problem of estimating
the radiation fluxes for the same sample of stars, but in
bands 2, 4, and 6, and compare our results with the existing
observational data. To this purpose, we approximated the emissivity of band 2 with the emissivity of band 3 and the emissivity of bands 4 and 6 with that of band 5. Our results are detailed in the supplemental material, Table S2. The deviation of our estimates for the radiation fluxes from those reported in the current literature is quantified by the relative error, \( \delta \), defined in Eq. (9).

To fully exploit the predictive power of our technique, in Figs. 5(e)–5(j), we compare the relative errors of the radiation fluxes \( \delta \), Eq. (9), respectively, with emissivity \( \varepsilon_\lambda \leq 1.0 \) and \( \varepsilon_\lambda = 1.0 \) in all six bands of the MSX catalog: (e) band 1, (f) band 2, (g) band 3, (h) band 4, (i) band 5, and (j) band 6.

The results discussed so far are based on data from the MSX catalog covering the infrared range 4.22–25.1 \( \mu m \). Our conclusions are also corroborated by a preliminary analysis of data from the Large Sky Area Multi-Object Fiber Spectroscopic Telescope (LAMOST) catalog in the optical range 0.37–0.9 \( \mu m \) [40,41]. We choose a sample of 50 stars. The emissivity turns out to be 1.00 in the wavelength range 0.555–0.69 \( \mu m \) (visible light) and 0.90 in the two side ranges, 0.32–0.38 (ultraviolet light) and 0.85–0.97 \( \mu m \) (near-infrared light). See the Appendix for details.

**F. Prediction of stellar radiation fluxes in bands without observational data**

The spectral emissivity calculated above can also be used to predict the radiation fluxes in spectral bands where
We finally remark that the comparison of the radiation flux data of Table S3 with future direct flux measurements will be straightforward, thanks to the accurate estimates of the corresponding band emissivity provided in the same table. Of course, this technique can be used to fill observational data gaps in any available star catalog.

**IV. CONCLUSIONS**

We have developed an inverse model to extract stellar band emissivity from astronomical observations. The “emissivity” mentioned in this article is the “effective emissivity,” defined as the ratio of the radiation emitted by the stellar surface to the radiation emitted by a standard blackbody at the same temperature. The stellar radiation fluxes in certain spectral bands serve as model input. The stochastic particle swarm optimization algorithm was implemented to optimize the model parameters, namely, spectral emissivity, effective temperature, and detection angular parameter, of the sampled stars. The close agreement between our predictions and the existing observational data is advocated to validate our method. Having implemented to optimize the model parameters, namely, spectral emissivity, effective temperature, and detection angular parameter, of the sampled stars. The close agreement between our predictions and the existing observational data is advocated to validate our method. Having implemented to optimize the model parameters, namely, spectral emissivity, effective temperature, and detection angular parameter, of the sampled stars. The close agreement between our predictions and the existing observational data is advocated to validate our method.

Making use of self-consistent estimates of the stellar spectral emissivity $\varepsilon_\lambda \leq 1.0$ is a more effective strategy than assuming stars as blackbody sources with $\varepsilon_\lambda = 1.0$. Finally, as a model application, our method predicts the radiation fluxes in spectral bands not populated by telescope observation data and for which only qualitative estimates have been proposed. This work provides an alternative way to estimate stellar emissivity.

**ACKNOWLEDGMENTS**

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FIG. 6. Statistics of the relative errors $\delta$ of the radiation fluxes with emissivity $\varepsilon_\lambda \leq 1.0$ and $\varepsilon_\lambda = 1.0$ in the different bands of the LAMOST catalog: (a) band 1, (b) band 2, (c) band 3, (d) band 4, and (e) band 5.

TABLE I. Calculation of temperatures and stellar radiation fluxes of 50 stars in band 1 (0.32–0.38 $\mu$m), band 3 (0.555–0.69 $\mu$m), and band 5 (0.85–0.97 $\mu$m) of the LAMOST catalog. $\varepsilon_\lambda$ is the emissivity of star at wavelength $\lambda$. $E_c$ is the calculated radiation flux (unit: $\times 10^{-19}$ W/m$^2$).

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<th>Band 1</th>
<th>Band 3</th>
<th>Band 5</th>
</tr>
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<td>$\varepsilon_\lambda$</td>
<td>$E_c$</td>
<td>$\varepsilon_\lambda$</td>
<td>$E_c$</td>
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<tr>
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(Table continued)
TABLE I. (Continued)

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<th>Band 5</th>
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<th>Temperature in the LAMOST catalog [62]</th>
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